# The $\mathbf{9}^{\text {th }}$ China-Russia Conference 

## on

## Knot Theory and Related Topics



August 15-19, 2023
Jilin University
Sino-Russian Mathematics Center


## Program Committee

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Vassily Manturov (Moscow Institute of Physics and Technology)
Sergei Matveev (Chelyabinsk State University)
Andrei Vesnin (Tomsk State University and Sobolev Institute of Mathematics)
Jiajun Wang (Peking University)
Zhiqing Yang (Dalian University of Technology)
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Ying Zhang (Soochow University)

# Hosting University 

Jilin University

## Supporting

Peking University
Regional Mathematical Center of Tomsk State University

$\bigcap$ MIPT.


## The 9th China-Russia Conference on Knot Theory and Related Topics

## Schedule (GMT+8, Beijing)

Aug 16, 2023 (Zhengxin Building 209. ZOOM: 89331384591; Code: 143467)

| Time | Speaker | Title | Chair |  |
| :---: | :---: | :---: | :---: | :---: |
| 08:30-08:50 | Opening Speeches and Group Photo |  |  |  |
| 08:50-09:40 | Andrei Vesnin | Invariants of spatial graphs and <br> associated links | Zhiyun Cheng |  |
| 09:50-10:40 | Tianyu Yuan | Morse theory of symmetric <br> products | Zhiyun Cheng |  |
| 10:40-11:00 | Tea Break |  |  |  |
| 11:00-11:50 | Zhiqing Yang | Graded knot polynomials | Zhiyun Cheng |  |
| 12:00 | Lunch |  |  |  |


| 14:00-14:50 | Igor Nikonov | On topological interpretation of universal parity-like labellings | Nikolay <br> Abrosimov |
| :---: | :---: | :---: | :---: |
| 15:00-15:50 | Andrei <br> Malyutin | Generalizations of Artin's theorem on isotopic closed braids | Nikolay <br> Abrosimov |
| 15:50-16:10 | Tea Break |  |  |
| 16:10-17:00 | Evgeny <br> Fominykh | Minimal ideal triangulations of 3-manifolds | Zhiqing Yang |
| 17:10-17:35 | Vuong Huu Bao | Twisted Alexander polynomial of knots in 3-torus | Zhiqing Yang |
| 17:35-18:00 | Roman Drybas | Ideal tetrahedra, photography principle and invariants of manifolds | Zhiqing Yang |
| 18:00 | Dinner |  |  |

Aug 17, 2023 (Zhengxin Building 209. ZOOM: 89331384591; Code: 143467)

| Time | Speaker | Title | Chair |  |
| :---: | :---: | :---: | :---: | :---: |
| 08:50-09:40 | Shengmao Zhu | On the asymptotic expansion for <br> the colored Jones polynomial of <br> twist knots | Jiajun Wang |  |
| 09:50-10:40 | Qingtao Chen | Recent progress of original <br> Volume Conjecture and its <br> generalizations | Jiajun Wang |  |
| 10:40-11:00 | Tea Break |  |  |  |
| 11:00-11:50 | Nikolay <br> Abrosimov | Euclidean volume of a cone <br> manifold over a hyperbolic knot <br> is always an algebraic number | Jiajun Wang |  |
| 12:00 | Lunch |  |  |  |


| 14:00-14:50 | Philipp <br> Korablev | Modular category with two <br> simple objects and corresponding <br> invariants of links and <br> 3-manifolds | Seongjeong <br> Kim |  |
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| 15:00-15:50 | Vassily <br> Manturov | The photography method | Seongjeong <br> Kim |  |
| 15:50-16:10 | Tea Break |  |  |  |
| 16:10-16:35 | Ziyi Lei | A Categorification for the Signed <br> Chromatic Polynomial | Xiao Wang |  |
| 16:35-17:00 | Andrei Egorov | Upper bounds for the volumes of <br> hyperbolic polyhedra and links | Xiao Wang |  |
| 17:10-17:35 | Maxim Ivanov | Virtual knot groups and circular <br> orderability | Xiao Wang |  |
| 17:35-18:00 | Liliya Grunvald | The number of rooted forests in a <br> circulant graph | Xiao Wang |  |
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Aug 18, 2023 (Zhengxin Building 209. ZOOM: 89331384591; Code: 143467)

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| 08:50-09:40 | Shijie Gu | Hypoabelian knot group and its <br> interaction with exotic <br> contractible manifolds | Andrei Vesnin |  |
| 09:50-10:40 | Zhongtao Wu | Alexander polynomial of spatial <br> graph | Andrei Vesnin |  |
| 10:40-11:00 | Tea Break |  |  |  |
| 11:00-11:50 | Valeriy <br> Bardakov | Yang-Baxter equation, relative <br> Rota-Baxter operators and skew <br> braces | Andrei Vesnin |  |
| $12: 00$ | Lunch |  |  |  |


| $14: 00-18: 00$ | Free Discussions |
| :---: | :---: |
| $18: 00$ | Dinner |

## The 9th China-Russia Conference on Knot Theory and Related Topics

## Schedule (GMT+7, Novosibirsk)

Aug 16, 2023 (Zhengxin Building 209. ZOOM: 89331384591; Code: 143467)

| Time | Speaker | Title | Chair |  |
| :---: | :---: | :---: | :---: | :---: |
| 07:30-07:50 | Opening Speeches and Group Photo |  |  |  |
| 07:50-08:40 | Andrei Vesnin | Invariants of spatial graphs and <br> associated links | Zhiyun Cheng |  |
| 08:50-09:40 | Tianyu Yuan | Morse theory of symmetric <br> products | Zhiyun Cheng |  |
| 09:40-10:00 | Tea Break |  |  |  |
| 10:00-10:50 | Zhiqing Yang | Graded knot polynomials | Zhiyun Cheng |  |
| 11:00 | Lunch |  |  |  |


| 13:00-13:50 | Igor Nikonov | On topological interpretation of <br> universal parity-like labellings | Nikolay <br> Abrosimov |  |
| :---: | :---: | :---: | :---: | :---: |
| 14:00-14:50 | Andrei <br> Malyutin | Generalizations of Artin's <br> theorem on isotopic closed braids | Nikolay <br> Abrosimov |  |
| 14:50-15:10 | Tea Break |  |  |  |
| 15:10-16:00 | Evgeny <br> Fominykh | Minimal ideal triangulations of <br> 3-manifolds | Zhiqing Yang |  |
| 16:10-16:35 | Vuong Huu <br> Bao | Twisted Alexander polynomial of <br> knots in 3-torus | Zhiqing Yang |  |
| 16:35-17:00 | Roman Drybas | Ideal tetrahedra, photography <br> principle and invariants of <br> manifolds | Zhiqing Yang |  |
| 17:00 | Dinner |  |  |  |

Aug 17, 2023 (Zhengxin Building 209. ZOOM: 89331384591; Code: 143467)

| Time | Speaker | Title | Chair |  |
| :---: | :---: | :---: | :---: | :---: |
| 07:50-08:40 | Shengmao Zhu | On the asymptotic expansion for <br> the colored Jones polynomial of <br> twist knots | Jiajun Wang |  |
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| 10:00-10:50 | Nikolay <br> Abrosimov | Euclidean volume of a cone <br> manifold over a hyperbolic knot <br> is always an algebraic number | Jiajun Wang |  |
| 11:00 | Lunch |  |  |  |


| 13:00-13:50 | Philipp <br> Korablev | Modular category with two <br> simple objects and corresponding <br> invariants of links and <br> 3-manifolds | Seongjeong <br> Kim |  |
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| 14:00-14:50 | Vassily <br> Manturov | The photography method | Seongjeong <br> Kim |  |
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| 15:10-15:35 | Ziyi Lei | A Categorification for the Signed <br> Chromatic Polynomial | Xiao Wang |  |
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| 16:10-16:35 | Maxim Ivanov | Virtual knot groups and circular <br> orderability | Xiao Wang |  |
| 16:35-17:00 | Liliya Grunvald | The number of rooted forests in a <br> circulant graph | Xiao Wang |  |
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Aug 18, 2023 (Zhengxin Building 209. ZOOM: 89331384591; Code: 143467)

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| 10:00-10:50 | Valeriy <br> Bardakov | Yang-Baxter equation, relative <br> Rota-Baxter operators and skew <br> braces | Andrei Vesnin |  |
| $11: 00$ | Lunch |  |  |  |


| $13: 00-17: 00$ | Free Discussions |
| :---: | :---: |
| $17: 00$ | Dinner |

The 9th China-Russia Conference on Knot Theory and Related Topics

## Schedule (GMT+3, Moscow)

Aug 16, 2023 (Zhengxin Building 209. ZOOM: 89331384591; Code: 143467)

| Time | Speaker | Title | Chair |  |
| :---: | :---: | :---: | :---: | :---: |
| 03:30-03:50 | Opening Speeches and Group Photo |  |  |  |
| 03:50-04:40 | Andrei Vesnin | Invariants of spatial graphs and <br> associated links | Zhiyun Cheng |  |
| 04:50-05:40 | Tianyu Yuan | Morse theory of symmetric <br> products | Zhiyun Cheng |  |
| 05:40-06:00 | Tea Break |  |  |  |
| 06:00-06:50 | Zhiqing Yang | Graded knot polynomials | Zhiyun Cheng |  |
| 07:00 | Lunch |  |  |  |


| 09:00-09:50 | Igor Nikonov | On topological interpretation of <br> universal parity-like labellings | Nikolay <br> Abrosimov |  |
| :---: | :---: | :---: | :---: | :---: |
| 10:00-10:50 | Andrei <br> Malyutin | Generalizations of Artin's <br> theorem on isotopic closed braids | Nikolay <br> Abrosimov |  |
| 10:50-11:10 | Tea Break |  |  |  |
| 11:10-12:00 | Evgeny <br> Fominykh | Minimal ideal triangulations of <br> 3-manifolds | Zhiqing Yang |  |
| 12:10-12:35 | Vuong Huu <br> Bao | Twisted Alexander polynomial of <br> knots in 3-torus | Zhiqing Yang |  |
| 12:35-13:00 | Roman Drybas | Ideal tetrahedra, photography <br> principle and invariants of <br> manifolds | Zhiqing Yang |  |
| 13:00 | Dinner |  |  |  |

Aug 17, 2023 (Zhengxin Building 209. ZOOM: 89331384591; Code: 143467)

| Time | Speaker | Title | Chair |  |
| :---: | :---: | :---: | :---: | :---: |
| 03:50-04:40 | Shengmao Zhu | On the asymptotic expansion for <br> the colored Jones polynomial of <br> twist knots | Jiajun Wang |  |
| 04:50-05:40 | Qingtao Chen | Recent progress of original <br> Volume Conjecture and its <br> generalizations | Jiajun Wang |  |
| 05:40-06:00 | Tea Break |  |  |  |
| 06:00-06:50 | Nikolay <br> Abrosimov | Euclidean volume of a cone <br> manifold over a hyperbolic knot <br> is always an algebraic number | Jiajun Wang |  |
| 07:00 | Lunch |  |  |  |


| 09:00-09:50 | Philipp <br> Korablev | Modular category with two <br> simple objects and corresponding <br> invariants of links and <br> 3-manifolds | Seongjeong <br> Kim |  |
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| 11:35-12:00 | Andrei Egorov | Upper bounds for the volumes of <br> hyperbolic polyhedra and links | Xiao Wang |  |
| 12:10-12:35 | Maxim Ivanov | Virtual knot groups and circular <br> orderability | Xiao Wang |  |
| 12:35-13:00 | Liliya Grunvald | The number of rooted forests in a <br> circulant graph | Xiao Wang |  |
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| 06:00-06:50 | Valeriy <br> Bardakov | Yang-Baxter equation, relative <br> Rota-Baxter operators and skew <br> braces | Andrei Vesnin |  |
| $07: 00$ | Lunch |  |  |  |


| 09:00-13:00 | Free Discussions |
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# s \& Abstracts 

## Nikolay Abrosimov

Tomsk State University, Tomsk; Sobolev Institute of Mathematics, Novosibirsk
Title: Euclidean volume of a cone manifold over a hyperbolic knot is always an algebraic number


#### Abstract

The hyperbolic structure on a 3-dimensional cone-manifold with a knot as singularity can often be deformed into a limiting Euclidean structure. In the present work [1] we show that the respective normalised Euclidean volume is always an algebraic number, which is reminiscent of Sabitov's theorem (the Bellows Conjecture). This fact also stands in contrast to hyperbolic volumes whose number-theoretic nature is usually quite complicated. This is a joint work with Alexander Kolpakov and Alexander Mednykh. References:


[1] N. Abrosimov, A. Kolpakov, A. Mednykh, Euclidean volumes of hyperbolic knots // Proceedings of AMS, 2023 (in press). DOI: 10.1090/proc/16353

## Vuong Huu Bao

Tomsk State University, Tomsk
Title: Twisted Alexander polynomial of knots in 3-torus
Abstract: This work is on some aspects of knots and links in three-dimensional torus. We consider the classical three-dimensional torus as quotient of a cube with identification of boundary faces. We study a diagrammatic approach for knots and links in the torus. We obtain a complete finite set of Reidemeister type moves for equivalence up to ambient isotopy. A presentation of fundamental group for the complement of a link in three-dimensional torus is given. Using Fox calculus, we obtain an algorithm, computing twisted Alexander polynomial for knots in 3-torus

## Valeriy Bardakov

Tomsk State University, Tomsk; Sobolev Institute of Mathematics, Novosibirsk Title: Yang-Baxter equation, relative Rota-Baxter operators and skew braces
Abstract: The Yang-Baxter equation (YBE) is a fundamental equation in mathematical physics that arises in quantum groups. It has applications in the study of exactly solvable models in statistical mechanics and quantum field theory, and has connections to knot theory and braid groups. It my talk I discuss connection the YBE with some algebraic systems. In particular, with skew braces, post-groups, Rota-Baxter operators and relative Rota-Baxter operators on groups. The last objects for groups were introduced in papers of Chinese mathematicians: Chengming Bai, Li Guo, H. Lang, Yunhe Sheng, Rong Tang.

## Qingtao Chen

NYU Abu Dhabi
Title: Recent progress of original Volume Conjecture and its generalizations
Abstract: The original Volume Conjecture of Kashaev-Murakami-Murakami predicts a precise relation between the asymptotics of the colored Jones polynomials of a knot in $S^{\wedge} 3$ and the hyperbolic volume of its complement.

I will first discuss two different directions that lead to generalizations of this conjecture. The first direction concerns different quantum invariants of knots, arising from the colored $\operatorname{SU}(\mathrm{n})$ (with the colored Jones polynomial corresponding to the case $\mathrm{n}=2$ ). I will first display subtle relations between congruence relations, cyclotomic expansions and the original Volume Conjecture for colored Jones polynomials of knots. I will then generalize this point of view to the colored $\mathrm{SU}(\mathrm{n})$ invariant of knots. Certain congruence relations for colored SU(n) invariants, discovered in joint work with K. Liu, P. Peng and S. Zhu, lead us to formulate cyclotomic expansions and a Volume Conjecture for these colored SU(n) invariants. In 2021, joint with K. Liu and S. Zhu, we proved cyclotomic expansion for the colored $\operatorname{SU}(\mathrm{n})$ invariants of double twist knots. I will also discuss similar ideas for the superpolynomials that arise in HOMFLY-PT homology.
In fact, I proposed cyclotomic expansion conjectures and Volume conjectures for superpolynomials.

Another direction for generalization involves the Witten-Reshetikhin-Turaev and the Turaev-Viro quantum invariants of 3 -manifolds. In a joint work with T. Yang, we formulated a new Volume Conjecture for the asymptotics of these 3-manifolds invariants evaluated at certain roots of unit, and numerically checked it for many examples. Interestingly, this conjecture uses roots of unity that are different from the one usually considered in literature. This may indicate that the understanding of this new phenomenon requires new physical and geometric interpretations that go beyond the usual quantum Chern-Simons theory. I will also introduce a work on Krillov-Reshetikhin quantum 6j-symbols done by J. Murakami \& me.

Finally I will explain how we prove the original Volume Conjecture for twist knots K_\{p\} with $p>=6$. This is a recent joint work Shengmao Zhu.

## Roman Drybas

Moscow Institute of Physics and Technology
Title: Ideal tetrahedra, photography principle and invariants of manifolds
Abstract: We apply the photography principle for hyperbolic 2-3 Pacner move to construct invariants of 4-manifolds.

## Andrei Egorov

Sobolev Institute of Mathematics, Novosibirsk
Title: Upper bounds for the volumes of hyperbolic polyhedra and links
Abstract: By virtue of Belletti's theorem, the upper exact bound for volumes of generalized hyperbolic polyhedra having the same 1-skeleton $G$ is achieved on an ideal right-angled polyhedron whose 1 -skeleton is the medial graph of the graph $G$. We will talk about the volume estimates for generalized hyperbolic polyhedra that can be obtained using this result. Also, we will talk about new upper bounds for the volumes of hyperbolic links in terms of the number of twists in the diagram.

## Evgeny Fominykh

Saint Petersburg University
Title: Minimal ideal triangulations of 3-manifolds
Abstract: Recent developments in the theory of complexity for 3-manifolds are reviewed. New methods for computing complexity are described, based on calculation of the Turaev-Viro invariants and homologies of 3-manifolds. This research was supported by the Russian Science Foundation under project no. 22-21-00747.

## Liliya Grunwald

Sobolev Institute of Mathematics, Novosibirsk
Title: The number of rooted forests in a circulant graph
Abstract: In the paper [1], we develop a new method to produce explicit formulas for the number $f_{-} G(n)$ of rooted spanning forests in the circulant graphs $G=C_{n}\left(s_{1}, s_{2}, \ldots, s_{k}\right)$ and $\mathrm{G}=\mathrm{C}_{2 \mathrm{n}}\left(\mathrm{s}_{1}, \mathrm{~s}_{2}, \ldots, \mathrm{~s}_{\mathrm{k}}, \mathrm{n}\right)$. These formulas are expressed through Chebyshev polynomials. We prove that in both cases the number of rooted spanning forests can be represented in the form $f_{G(n)}=p a(n)^{2}$, where $a(n)$ is an integer sequence and $p$ is a certain natural number depending on the parity of $n$. Finally, we find an asymptotic formula for $f_{G(n)}$ through the Mahler measure of the associated Laurent polynomial.This is joint work with Ilya Mednykh.

## References:

[1] L. Grunwald, I. Mednykh, The number of rooted forests in circulant graphs // Ars Mathematica Contemporanea, 22 (2022) \#P4.10. DOI: 10.26493/1855-3974.2029.01d

## Shijie Gu

Northeastern University
Title: Hypoabelian knot group and its interaction with exotic contractible manifolds Abstract: A group is said to be hypoabelian if it contains no nontrivial perfect subgroup. In this talk, we will introduce knot groups which are hypoabelian. As an application, we will use hypoabelian knot groups to understand the behavior of fundamental groups at infinity of exotic contractible manifolds.

## Maxim Ivanov

Sobolev Institute of Mathematics, Novosibirsk
Title: Virtual knot groups and circular orderability
Abstract: A group $G$ is called left-orderable if there is a total order on $G$ that is invariant under left multiplication. All classical knot groups are left-orderable by the famous theorem of Howie and Short. We will discuss left-orderability of virtual knot group and a weaker property of circular orderability.

## Philipp Korablev

Chelyabinsk State University, Chelyabinsk
N.N. Krasovskii Institute of Mathematics and Mechanics of the UB RAS, Ekaterinburg

Title: Modular category with two simple objects and corresponding invariants of links and 3-manifolds


#### Abstract

In this talk we will describe the modular category E with two simple objects. This category is not new. It often appears as the simplest modular category with non-trivial associativity isomorphisms. We will explicitly describe all necessary structural morphisms (braiding, twist and duality) in this category. Then we will use the Turaev functor to extract invariants for non-oriented links in 3-sphere and closed 3-manifolds. As an example, we will obtain an explicit formula for the value of this invariant for lense spaces. Next, we will use a well-known procedure to extract a Turaev - Viro type invariant from category E. Finally, we will show that this invariant coincides with the well-known epsilon invariant for 3-manifolds.


## Ziyi Lei

Beijing Normal University
Title: A Categorification for the Signed Chromatic Polynomial
Abstract: By coloring a signed graph by signed colors, one obtains the signed chromatic polynomial of the signed graph. For each signed graph we construct graded cohomology groups whose graded Euler characteristic yields the signed chromatic polynomial of the signed graph. We show that the cohomology groups satisfy a long exact sequence which categorifies the signed deletion-contraction rule. This work is motivated by Helme-Guizon and Rong's construction of the categorification for the chromatic polynomial of unsigned graphs.

## Andrei Malyutin

St. Petersburg Department of Steklov Mathematical Institute, St. Petersburg
Title: Generalizations of Artin's theorem on isotopic closed braids
Abstract: A classical theorem of braid theory dating back to Artin's works says that two closed braids in a solid torus are ambient isotopic if and only if they represent the same conjugacy class of the braid group. We obtain several generalizations of this theorem. In particular, we show that transversal links in an arbitrary compact orientable 3-manifold fibered over the circle with a compact fiber are ambient isotopic if and only if they are isotopic in the class of transversal links. These generalizations allow us to obtain new estimates for the number of knots with a given arc index.

## Vassily Manturov

Moscow Institute of Physics and Technology
Title: The photography method
Abstract: We formulate a general method allowing one to

1) solve various equations
2) construct invariants of topological objects
by using some very general notion of data and data transmission law.

By data we mean, say, objects of geometric origin (lengths, areas, etc.), by data transmission law we mean some equations rewriting the data given in one system of coordinates in terms of some other system of coordinates(one key example is the Ptolemy equation).

Such considerations allow one to solve various equations "for free". We shall concentrate on obtaining invariants of braids 3-manifolds and 4-manifolds, solutions to the pentagon equaitons and representations of groups G_\{n\}^\{3\}.

This photography method ties together many branches in mathematics; in particular, our data transmission law is naturally related to see mutations in cluster algebras.
https://arxiv.org/abs/2305.06316
https://arxiv.org/pdf/2305.11945.pdf
https://arxiv.org/abs/2306.07079
https://arxiv.org/abs/2307.03437

## Igor Nikonov

Lomonosov Moscow State University
Title: On topological interpretation of universal parity-like labellings
Abstract: Some labellings of crossings compatible with Reidemeister moves like the universal parity and the universal index admit topological interpretation (homological parity and homotopical index). In the talk we present some other examples of topological interpretation of universal labellings on knot diagrams in a fixed surface.

## Andrei Vesnin

Tomsk State University, Tomsk
Title: Invariants of spatial graphs and associated links
Abstract: We will discuss spatial embeddings of graphs into the 3-sphere. Even a graph can be simple combinatorically, its embedding can be very complicated since any cycle of a graph will be embedded as a knot in the 3-sphere. Two spatial graphs are said to be equivalent if there is an ambient isotopy of the 3 -sphere which transforms one spatial graph to another. As well as knots and links, spatial graphs can be studied from their diagrams. The Yamada and Jagger polynomials are most useful invariants of spatial graphs. Let K 4 be the complete graph on 4 vertices. We will present a relation between normalized Jagger polynomials of spatial K4-graph and its spatial subgraphs with Jones polynomial of the associated link. The obtained results are joint with O. Oshmarina.

## Zhongtao Wu

The Chinese University of Hong Kong
Title: Alexander polynomial of spatial graph
Abstract: Alexander polynomial has been one of the most important tools in the development of knot theory since its discovery 100 years ago. For spatial graphs, Bao and the speaker defined an analogous invariant. In many aspects, the Alexander polynomial of spatial graphs shares similar topological properties with the classical one for knots; but it also contains certain unique graph theoretical information, such as, its evaluation at $t=1$ gives the number of spanning trees of the graph. This talk aims to give a general introduction to this invariant.

## Zhiqing Yang

Dalian University of Technology
Title: Graded knot polynomials
Abstract: Most knot polynomial invariants are not polynomial time computable. But after deforming the knot polynomial and dividing it according to certain grading, each component can be polynomial time computable. In this way, knot invariants that were previously very complex can now be calculated with their low-order components. This idea was applied to HOMFLY polynomial by mathematicians such as Jozef H. Przytycki, F. Jaeger, Akio Kawauchi and others. This report generalizes this result, showing that the knot polynomial deformation they give is a special case of the reporter's knot invariant, and discusses more general possibilities.

## Tianyu Yuan

Beijing International Center for Mathematical Research
Title: Morse theory of symmetric products
Abstract: We present an approach to do Morse theory on symmetric products of surfaces, and show its relation to higher-dimensional Heegaard Floer homology (HDHF). As an application, we recover the finite Hecke algebra by Morse theory. We also sketch the application to spectral networks. This is joint work with Ko Honda and Yin Tian.

## Shengmao Zhu

Zhejiang Normal University
Title: On the asymptotic expansion for the colored Jones polynomials of twist knots Abstract: In this talk, I will present an asymptotic expansion for the colored Jones polynomial for twist knots at the $\mathrm{N}+1 / 2$-th roots of unity by using the saddle point method developed by Ohtsuki. As a corollary, we prove a version of volume conjecture proposed by Detcherry-Kalfagianni-Yang for twist knot K_p with $\mathrm{p}>=6$. This is a joint work with Qingtao Chen.

## Participants

| Nikolay Abrosimov | Tomsk State University <br> Sobolev Institute of Mathematics |
| :--- | :--- |
| Darya Aksenova | St. Petersburg Department of Steklov Mathematical <br> Institute |
| Ilya Alekseev | Saint Petersburg University |
| Vuong Huu Bao | Tomsk State University |
| Valeriy Bardakov | Tomsk State University, <br> Sobolev Institute of Mathematics |
| Anna Chelnokova | Tomsk State University |
| Liang Chen | Northeast Normal Universty |
| Qingtao Chen | NYU Abu Dhabi |
| Zhiyun Cheng | Beijing Normal University |
| Siqi Ding | Dalian University of Technology |
| Roman Drybas | Moscow Institute of Physics and Technology |
| Dmitriy Drozdov | Novosibirsk State University |
| Qiang E | Dalian Maritime University |
| Andrei Egorov | Sobolev Institute of Mathematics |
| Vladimir Evteev | Tomsk State University |
| Bing Fang | Dalian University of Technology |
| Evgeny Fominykh | Saint Petersburg University |
| Yue Gao | Anhui Normal University |
| Liliya Grunewald | Sobolev Institute of Mathematics |
| Shijie Gu | Northeastern University |
| Maxim Ivanov | Sobolev Institute of Mathematics, Novosibirsk |
| Seongjeong Kim | Jilin University |
| Philipp Korablev | Chelyabinsk State University |
| Tatyana Kozlovskaya | Tomsk State University |
| Ziyi Lei | Beijing Normal University |
| Xudong Leng | Liaoning Normal University |
| Miaowang Li | Dalian Maritime University |
| Ping Li | Fudan University |
| Xiang Liu | Academy of Mathematics and Systems Science Chinese <br> Academy of Sciences <br> Institute |
| Jiming Ma | Fudan University |
| Liyuan Ma | Dalian University of Technology |
| Sergei Maksimovich | Novosibirsk State University |
| Andrey Malyutin | St. Petersburg Department of Steklov Mathematical <br> Institute |
| Vassily Manturov | Moscow Institute of Physics and Technology |
| Alexey Miller | Setersbrg Depart of Steklov Mathematical |


| Daniil Nigomedyanov | Saint Petersburg University |
| :--- | :--- |
| Igor Nikonov | Lomonosov Moscow State University |
| Olga Oshmarina | Novosibirsk State University |
| Anton Ryabkov | Saint Petersburg University |
| Maxim Semashko | Tomsk State University |
| Guangyan Shen | Northeast Normal University |
| Yunhe Sheng | Jilin University |
| Pavel Sokolov | Novosibirsk State University |
| Galina Sokolova | Novosibirsk State University |
| Dongqi Sun | Harbin Engineering University |
| Andrei Vesnin | Tomsk State University and Sobolev Institute of <br> Mathematics |
| Jiajun Wang | Peking University |
| Jun Wang | Hebei Normal University |
| Xiao Wang | Jilin University |
| Jianchun Wu | Soochow University |
| Zhongtao Wu | The Chinese University of Hong Kong |
| Mengian Xu | Guangxi Normal University |
| Zhiqing Yang | Dalian University of Technology |
| Tianyu Yuan | Beijing International Center for Mathematical Research |
| Ivan Yudin | Sobolev Institute of Mathematics |
| Faze Zhang | Northeast Normal University |
| Qiang Zhang | Xi'an Jiaotong University |
| Yimu Zhang | Jilin University |
| Shengmao Zhu | Zhejiang Normal University |
| Kseniya Zimireva | Novosibirsk State University |
| Matvei Zonov | Novosibirsk State University |

## Maps and Directions

## Yandu Hotel to Zhengxin Building



About 750 meters, 10mins by walk.

## Zhengxin Building to Danianchuyi



About 800 meters, 12 mins by walk.

## Danianchuyi to Yandu Hotel



About 1.6 km, 25mins by walk.

